LLNL-Earth3D User Manual

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Table of Contents

1. Introduction	1
1.1 General Background	1
1.2 References	4
2. Getting Started	5
_	6
3.1 Ray tracing input options	7
3.2 Ray tracing output options	
	9
<u>-</u>	13
4.1 General queries 1	13
4.2 Profiles and cross sections	
4.3 Map output 1	
5. Model importation.	

1. Introduction

LLNL-Earth3D is a computer code designed to support the use of the LLNL-G3D series of models (see *Simmons et al.* 2011, 2012). The primary purpose of the code is to compute 3-D ray paths for various body waves and calculate travel times between a seismic source and a seismic station. The code navigates the hierarchical spherical tessellation framework of the LLNL-G3D models and is multithreaded so that a number of ray paths and travel times can be computed concurrently. LLNL-Earth3D is also a more general model interface allowing for model property output, such as seismic velocity and the depth (or radius) of velocity discontinuities.

The LLNL-Earth3D code is written in Java and will work on any system with Java version 1.6.0 or higher. LLNL-Earth3D has been tested at LLNL on Windows, Linux, OS-X, and SUN systems.

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1.1 General Background

LLNL-Earth3D allows for fast calculation of 3-D seismic travel times and ray paths through a 3-D model of the Earth specifically represented with the LLNL-G3D global-scale model architecture. The model architecture is node-based and consists of a series of surfaces that may undulate (*not necessarily spherical*). Therefore, Earth's ellipticity and undulating discontinuity surfaces (such as the Moho) are explicitly represented. Each model surface is defined by a set of nodes evenly distributed around the globe, and multiple model properties (e.g. Vp, Vs, Q, etc.) may be defined at each node for a given

surface. The positioning (latitude and longitude) of the model nodes are defined by the vertices (or intersections) of the spherical tessellation grids (Figure 1). The spherical tessellation grids are created by recursive subdivision of triangular faces on a spherical surface. Each recursive subdivision of a tessellation grid generates higher resolution surfaces and a new level in the tessellation hierarchy which may be exploited for fast model referencing (see *Simmons et al.*, 2011).

To represent undulating (aspherical) surfaces, nodes are placed at arbitrary radii along geocentric vectors defined from the center of the Earth through the spherical tessellation vertices (Figure 2). Three-dimensional piecewise linear interpolation between nodes and surfaces is used to determine the value of model parameters at any arbitrary location. Discontinuities (e.g. the Moho) are represented with two surfaces defined at the same location, but with differing values (such as velocity) assigned to the top-side and bottom-side sets of nodes.

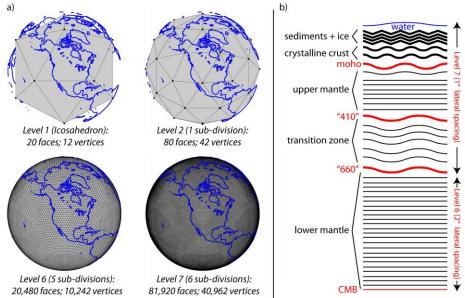


Figure 1. Summary of the LLNL-G3D model architecture. a) Selected levels of the spherical tessellation grids that define the location of nodes in the lateral extent. Nodes are placed at arbitrary radii in the direction of geocentric vectors pointing from the center of the Earth to the vertices. b) Description of the model surfaces in the LLNL-G3Dv3 P-wave model (*Simmons et al.*, 2012). Wavy lines correspond to surfaces that undulate and thick lines correspond to double surfaces needed to honor discontinuities. Flat lines correspond to surfaces that do not undulate, but note that all surfaces conform to the expected hydrostatic shape of the Earth (none of the surfaces are flat or spherical). The figure is from *Simmons et al.* (2012).

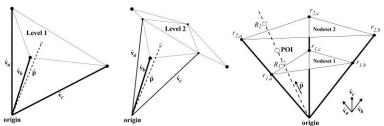


Figure 2. Model referencing and node architecture. (**a-b**) A hierarchical triangle searching algorithm is used to establish the vertices that surround a unit vector in the direction of the point-of-interest, $\hat{\bf p}$. Barycentric coordinates (triangular weights) are inherently determined at each step in the hierarchical search providing lateral interpolation weights at all tessellation levels. (**c**) Model nodes are placed at arbitrary radii in the direction of the vertices allowing for representation of irregular surfaces. To determine radial interpolation weights, radial profiles are determined along $\hat{\bf p}$ by lateral interpolation of radii for surrounding points (R_I interpolated from $r_{I,a-c}$ and R_2 interpolated from $r_{2,a-c}$). The distances of R_I and R_2 from the point-of-interest (POI) provide the simple radial interpolation weights, and any model property can then be determined. The figure is from *Simmons et al.* (2011).

Three-dimensional ray tracing is performed through the complex model using a modified version of the *Zhao et al.* (1992) method that uses pseudobending within the continuous part of the media while honoring Snell's law at discontinuous interfaces (Figure 3). The ray tracing modifications include methods to overcome local travel time minima issues and the ability to find multiple paths for regional phases that arrive within some time tolerance ("multi-pathing"). For more detailed information regarding model architecture and modeling procedures see *Myers et al.* (2011), *Simmons et al.* (2011), and *Simmons et al.* (2012).

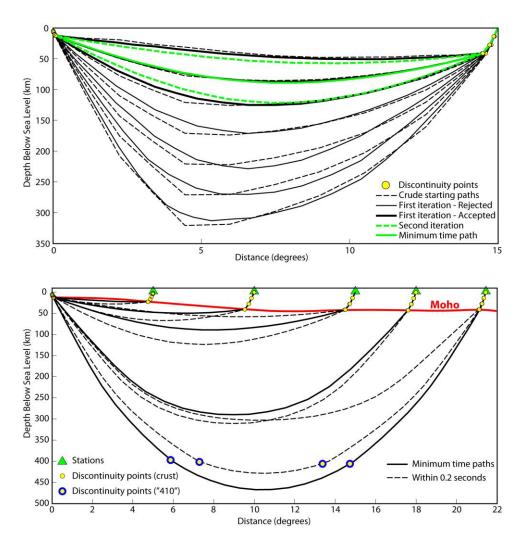


Figure 3. Three-dimensional ray tracing procedure adapted from Zhao et al. [1992] and seismic sensitivity definitions. (top) Several trial ray paths are tested to seek out the global minimum travel time. We perform a limited number of pseudo-bending [*Um and Thurber* 1987] and piercing point adjustment iterations on a set of simple starting paths (black dashed lines). Ray paths that provide travel times within some time tolerance (black solid lines) are further refined through bending and piercing point adjustments until only slight improvement (reduction) in travel times is observed (green dashed and solid lines). The minimum time path can then be selected from the set (green solid line). (bottom) Example 3-D ray paths calculated through the global velocity model constructed in *Simmons et al.* (2011).

1.2 References:

- Myers, S.C., G. Johannesson, and N.A. Simmons (2011). Global-scale P-wave tomography optimized for prediction of teleseismic and regional travel times for Middle East events: 1. Data set Development, *J. Geophys. Res.*, **116**, B04304, doi:10.1029/2010JB007967.
- Simmons, N.A, S.C. Myers, G. Johannesson (2011). Global-scale P-wave tomography optimized for prediction of teleseismic and regional travel times for Middle East events: 1. Tomographic inversion. *J. Geophys. Res.*, **116**, B04305, doi:10.1029/2010JB007969.
- Simmons, N.A, S.C. Myers, G. Johannesson, and E. Matzel (2012). LLNL-G3Dv3: Global P wave tomography model for improved regional and teleseismic travel time prediction. *J. Geophys. Res.*, **117**, B10302, doi:10.1029/2012JB009525.
- Um, J. and C. Thurber (1987). A fast algorithm for two-point seismic ray tracing, *Bull. Seis. Soc. Amer.*, **77**, 972-986.
- Zhao, D., A. Hasegawa, and S. Horiuchi (1992). Tomographic imaging of P and S wave velocity structure beneath northeastern Japan, *J. Geophys. Res.*, **97**, 19,909–19,928, doi:10.1029/92JB00603.

2. Getting Started

The LLNL-Earth3D code is written in Java and will work on any system with Java version 1.6.0 or higher. LLNL-Earth3D has been tested at LLNL on Windows, Linux, OS-X, and SUN systems. The LLNL-Earth3D .jar file may be executed by:

```
java -jar LLNL-Earth3D.x.x.jar
```

where "x.x" is a generic version number. If memory allocations for your platform are insufficient, you may need to execute by adding flags:

```
java -jar -ms1500m -mx1500m LLNL-Earth3D.x.x.jar
```

Executing the .jar without any arguments will create a user prompt:

```
E3D (input command):
```

After which you will enter command line options, described below. The program will continue to take user input until the user types the command "exit" or "quit", e.g.:

```
E3D (input command): quit
```

Alternatively, a single command can be run by including the arguments in the command line. For example:

```
java -jar LLNL-Earth3D.x.x.jar -getlayerinfo earthmodel
```

In the above command, the major operation is to list information about the layers in in the binary earth model, which may be a complete path pointing to a binary formatted earth model file. The code will execute this command, then exit LLNL-Earth3D. This option is used to facilitate LLNL-Earth3D being called by external programs.

All major operations are executed with switches (such as -getlayerinfo shown above) immediately following the .jar file name or at the beginning of the command prompt, depending on your execution style.

NOTE: Working from the prompt is more efficient if multiple operations are to be performed using a single earth model since the command line version requires loading a model into memory each time. Alternatively, a list of arguments from a text file could be passed simultaneously with the -arglist switch.

To get help regarding usages and the utilities available in the local .jar version, simply type -help at the E3D user prompt or, if LLNL-Earth3D is not initiated, type:

```
java -jar LLNL-Earth3D.x.x.jar -help
```

3. Ray tracing

Basic usage (output travel times only)

LLNL-Earth3D was originally designed to compute 3-D ray paths and travel times for many source-receiver pairs simultaneously, and as efficient as possible. Therefore, a plain text file containing rows with event locations, station locations, and phases is passed to the code. The event-station-phase rows are then distributed using multi-threading techniques.

To ray trace with default options, the general command is:

```
java -jar LLNL-Earth3D.x.x.jar -raytrace earthmodel events_stations_phases
```

or, from the command prompt:

```
E3D (input command): -raytrace earthmodel events_stations_phases
```

The variables are filenames pointing to the binary earth model (*earthmodel*) and the event-station-phase list (*events_stations_phases*). The event-station-phase list can have as many rows (entries) as desired and each row is formatted as follows:

```
[event_lat event_lon event_depth station_lat station_lon station_elevation phase extra...]
```

The *event_depth* and *station_elevation* are relative to a reference surface defined in the model (mean sea level for LLNL-G3Dv3 and other LLNL models). *phase* is a phase name such as P or Pn, etc. *extra* can be any additional columns of information the user wishes to include.

The default output will be a file named *events_stations_phases* with the added extension ".TT" which stands for <u>Travel Times</u>. The .TT file will contain all of the information in each row of the input file plus additional columns of output like the following:

```
[...input EARTH3D traveltime water_corr_ev water_corr_st arc_distance azimuth uniqueID]
```

Each line of output will have the word "EARTH3D" after the input columns if the code was able to ray trace the path, and the word "NULL" if it could not. The travel time (*traveltime*) follows EARTH3D and then an event-side water correction (*water_corr_ev*) and a station-side water correction (*water_corr_st*). Water corrections arise when an event or station appear to be in the water due to the resolution limitations of a given model. This happens quite often for ocean-island stations. If it is known that the event was not in the water, simply **add** the *water_corr_ev* term to the *traveltime* to get the total travel time. Likewise, if it is known that the station is in fact on solid land, add the *water_corr_st* term to the *traveltime* to get the total travel time.

Additional outputs include the event-station arc distance in degrees ($arc_distance$), the event-to-station azimuth (azimuth) and a unique identifier (uniqueID). The uniqueID are integers starting with zero that correspond to the row number of the input since the row ordering provided in the input file may not be preserved. The reordering occurs due to the multi-threading process which distributes each of the rows to multiple processors that complete the tasks at differing rates.

3.1 Ray tracing input options

Seismic phases

LLNL-Earth3D will attempt to compute travel times for a variety of phases. The user simply must identify the desired phase in each line of the *events_stations_phases* file. To get a current list of available seismic phases along with descriptions, type -listphases at the command prompt or:

java -jar LLNL-Earth3D.x.x.jar -listphases

<u>Note:</u> While some phases are relatively simple and have been tested more thoroughly than others (e.g. first arriving P and S waves), some other phases are more complex and may be unrealistic in extreme model regions and with difficult event-receiver configurations.

Travel time tolerances

For some seismic phases, the ray tracing algorithm begins with a *single* crude estimate of the path, then refines it according the pseudobending/Snell's law technique to find the minimum-time path. However, some phases (usually regional) require *several* initial paths to test and refine. For these more complex phases, the set of initial paths are partially optimized and down-selected to a smaller set of paths based on some initial time tolerance (*tolerance1*). The remaining paths are further refined and down-selected a final time based on a secondary time tolerance (*tolerance2*). See Figure 3 for a visual description. If the second tolerance (*tolerance2*) is greater than zero, it is possible that multiple paths are found to be within the given tolerance of the minimum time. In these cases, multiple paths are returned to the .TT file and path files if requested.

To adjust these tolerances, the user may put two numbers representing the two tolerances (in seconds) on the input line **immediately after** the event-station file:

E3D (input command): -raytrace earthmodel events_stations_phases tolerance1 tolerance2

The default tolerances are 2 and 0 seconds, respectively. Increasing the first tolerance (*tolerance1*) will allow more rays to be passed to the second phase for further optimization. Increasing the second tolerance (*tolerance2*) above zero will possibly result in multiple paths and travel times for some phases, whereas a second tolerance equal to 0 will return the minimum-time path.

Multi-threading

The default behavior when ray tracing is seek out the number of available processors (Nproc) on the working platform and create Nproc+2 threads since this is found to be most efficient. This default can be changed by adding the –nthreads switch followed by the number of threads desired:

E3D (input command): -raytrace earthmodel events_stations_phases tolerance1 tolerance2 -nthreads N

where *N* is the number of threads. Note that the tolerance values do not need to be specified if the default values are satisfactory:

E3D (input command): -raytrace earthmodel events_stations_phases -nthreads N

3.2 Ray tracing output options

Screen output

Simply include the switch -verbose or -v to output travel time results to the screen.

Output ray paths

When ray tracing, LLNL-Earth3D always outputs a travel time file (*.TT) by default. In addition, there are options for outputting ray paths. To output the full ray paths to files, add the switches -p or -paths after the ray tracing command:

E3D (input command): -raytrace earthmodel events stations phases -paths

Note that multiple switches (such as -nthreads *N*) can be included as well. The above command will output an ASCII file for each row of the *events_stations_phases* unless a particular path calculation was unsuccessful for any reason.

Each of the path file names will begin with input file name (*events_stations_phases*) with the added extension that includes the unique identifier (row number from the input file beginning with 0) followed by ".ascii.path". For example, if the input file name is "myRays.txt", the first output path file name will be "myRays.txt.0.ascii.path" and the 2nd file name will be "myRays.txt.1.ascii.path", etc.

Each of the path files will contain a header containing the output travel time information, the number of paths computed, the number of points in each path, and the path points. Each point along the path (each row after the header) will have the following format:

[point_lat point_lon point_radius point_distance point_depth]

where *point_distance* is the distance from the event origin to each point along the path (in km). If the actual coordinates of the paths are not needed, another option is to output only the *point_distance* and *point_radius* using the -distradius or -dr flag:

E3D (input command): -raytrace earthmodel events_stations_phases -distradius

Similar to the -paths output, each distradius file will have a header followed by points that are represented by only 2 columns in this case ([point_distance point_radius]). Filenames will have indexes just like the .path files, but end with ".distradius" as an extension.

3.3 Examples

Example 1a: Travel times

In this example, travel times for a small suite of P-wave phases will be computed using the LLNL-G3Dv3 model from Simmons et al. (2012).

Suppose we have created a text file named "myRays.txt" which contains:

The first 7 columns contain the required elements including earthquake latitude/longitude and depth (first 3 elements), the required station latitude/longitude and elevation (next 3 elements), and the seismic phase. The user may add additional columns that will not be used for ray tracing.

Here is an example -raytrace command to find the minimum-time paths:

```
java -jar Earth3D.5.3.jar -raytrace LLNL-G3Dv3.e3d.binary G:\PROGRAMS\EARTH3D\myRays.txt -verbose
```

Since we are not running from the prompt, the model (which also contains the hierarchical tessellation grids and pre-computed data used for ray tracing) will be loaded. The loading process requires some wait time and you will see:

Calculating Cross Products and Arc Distances...
Finding Triangle Centroids...
...
1: Water (top) added
reading layer[0] 1: Water (top)
2: Water (bottom) added
reading layer[1] 2: Water (bottom)
3: Sediment 1 (top) added
reading layer[2] 3: Sediment 1 (top)
4: Sediment 1 (bottom) added
...
Inner Core (6371km) added
reading layer[94] Inner Core (6371km)
completed earthmodel file read

Once the model is loaded, the lines of the "myRays.txt" will be read and ray tracing will commence. If the -verbose flag is included, the travel time output will be displayed on the screen. In any case, a file named "myRays.txt.TT" will now exist in the current working directory. The .TT file will have the contents:

```
Earth3D.5.3 -raytrace LLNL-G3Dv3.e3d.binary G:\PROGRAMS\EARTH3D\myRays.txt 2.0 0.0 -v
33.9000 -117.0500 12.1000 33.6100 -116.4600 1.2800 Pg event2 EARTH3D 10.756 0.000 0.000 0.57034 120.31098 3
37.6800 -121.7700 4.5000 -17.7400 178.0500 0.8010 P event1 EARTH3D 726.094 0.000 -0.886 78.94891 237.40205 2
37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.598 0.000 0.000 5.93075 131.63000 0
37.6800 -121.7700 4.5000 57.7800 -152.5800 0.1500 PcP extra info EARTH3D 547.156 0.000 -0.191 28.47414 324.86188 1
-29.9000 25.1300 35.7000 33.6100 -116.4600 1.2800 PKPdf ev3 EARTH3D 1177.306 0.000 0.000 147.25546 286.55142 4
```

The top line of the .TT file will have the ray tracing command line inputs that were entered (default travel time tolerances 2 and 0 will appear if none were entered). Each row will contain the original rows of the input file along with the LLNL-Earth3D results after the "EARTH3D" text. The elements of output include the travel time, event- and station-side water corrections, arc distance, azimuth, and unique identifiers (last column). See the beginning of the Ray tracing section for more description. In this case, the first row of the input was the Pn phase, but output is written on the 3rd data row due to the multi-threading. If desired, the rows can be resorted to the original order using the unique identifier.

Example 1b: Minimum-time path output

The previous example did not save the actual ray paths. This example will be an extension of the previous example and demonstrate how to output ray paths to ASCII files. We will work from the command prompt to avoid loading in the model again:

```
E3D (input command): -raytrace LLNL-G3Dv3.e3d.binary G:\PROGRAMS\EARTH3D\myRays.txt -paths
```

Note that we have added the -paths flag. This will generate 5 files, 1 path file for each row in the input file. The path file corresponding with the first row of the input file will be named "myRays.txt.0.ascii.path". The contents of this file will look like:

```
>
    37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.598 0.000 0.000 5.93075 131.63000 0
> npaths: 1 thispath: 1
> 221
  37.6800
             -121.7700
                          6365.6574
                                         0.0000
                                                       4.5000
             -121.7642
                          6365.0248
                                         0.7009
  37.6757
                                                       5.1342
             -121.7585 6364.3923
  37.6713
                                         1.4020
                                                      5.7683
          -121.7527 6363.7598
                                        2.1033
  37.6670
                                                      6.4023
  37.6626
            -121.7469 6363.1274
                                        2.8046
                                                      7.0362
            -121.7412
  37.6583
                         6362.4951
                                        3.5061
                                                      7.6701
  ...omitted...
  33.6104
          -116.4604 6371.8688 659.4132
                                                      -0.2792
                         6371.9291
6371.9894
                                                      -0.3394
  33.6102
             -116.4602
                                        659.4410
  33.6100
          -116.4600
                                        659.4689
                                                      -1.2800
```

The first character of each header line is ">" so that all path files can be concatenated together and plotted with one GMT psxy command. The travel time output is included in the header along with the number of ray paths that were found. There are 221 points in this path and the columns include latitudes, longitudes, radii, distances along the path, and depth.

Example 1c: Multi-paths

The previous example only output the minimum-time path for each row of the event-station-phase input file. This example will be an extension of the previous example and demonstrate how to output multiple ray paths with travel times within some tolerance of the minimum-time path. Working from the prompt, type:

```
E3D (input command): -raytrace LLNL-G3Dv3.e3d.binary G:\PROGRAMS\EARTH3D\myRays.txt 4 0.5 -distradius
```

In the above command, we have changed the first travel time tolerance to 4 seconds and the second time tolerance to 0.5 seconds. In this case, ray paths that arrive within 0.5 seconds of the minimum-time path found will be returned for some local and regional seismic phases such as Pg and Pn. The file named "myRays.txt.TT" will be replaced with:

```
Earth3D.5.3 -raytrace LLNL-G3Dv3.e3d.binary G:\PROGRAMS\EARTH3D\myRays.txt 4.0 0.5 -dr
  33.9000 -117.0500 12.1000 33.6100 -116.4600 1.2800 Pg event2 EARTH3D 10.800 0.000 0.57034 120.31098
  33.9000 -117.0500 12.1000 33.6100 -116.4600 1.2800 Pg event2 EARTH3D 10.817 0.000 0.000 0.57034 120.31098
  33.9000 -117.0500 12.1000 33.6100 -116.4600 1.2800 Pg event2 EARTH3D 10.756 0.000 0.000 0.57034 120.31098
  33.9000 -117.0500 12.1000 33.6100 -116.4600 1.2800 Pg event2 EARTH3D 10.819 0.000 0.000 0.57034 120.31098
  37.6800 -121.7700 4.5000 -17.7400 178.0500 0.8010 P event1 EARTH3D 726.094 0.000 -0.886 78.94891 237.40205
                                                                  EARTH3D 547.156 0.000 -0.230 28.47414 324.86188 1
  37.6800 -121.7700 4.5000 57.7800 -152.5800 0.1500 PcP extra info
  37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.598 0.000 0.000 5.93075 131.63000
  37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.633 0.000 0.000
  37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.750 0.000 0.000
                                                                                            5.93075 131.63000
  37.6800 -121.7700 4.5000
                                            1.2800 Pn user data EARTH3D 87.951 0.000 0.000
                                                                                                                 0
                           33.6100 -116.4600
                                                                                             5.93075
                                                                                                     131.63000
 -29.9000 25.1300 35.7000 33.6100 -116.4600 1.2800 PKPdf ev3 EARTH3D 1177.306 0.000 0.000 147.25546
                                                                                                     286.55142
```

Note that the Pg and Pn phases have multiple entries with slightly different travel times. These multiple entries possibly indicate "true" multipathing, but *there is no guarantee that the multi-paths are significantly different*. In other words, multiple starting paths could have converged to essentially the same path.

Rather than requesting paths with the -paths flag, we requested simplified path outputs with the -distradius command (which may be shortened to "-dr"). Similar to the full path output, this will generate 5 files (1 for each event-station-phase entry). The first file will be named "myRays.txt.0.distradius" and will look like:

```
37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.598 0.000 0.000 5.93075 131.63000 0
> npaths: 4 thispath: 1
> 221
   0.0000
           6365.6574
   0.7009 6365.0248
           6364.3923
   1.4020
   2.1033
           6363.7598
...omitted...
 659.3853
           6371.8085
           6371.8688
6371.9291
 659.4132
 659.4410
 659.4689 6371.9894
    37.6800 -121.7700 4.5000 33.6100 -116.4600 1.2800 Pn user data EARTH3D 87.633 0.000 0.000 5.93075 131.63000 0
> npaths: 4 thispath: 2
> 221
   0.0000
            6365.6574
   0.7102
            6365.0248
   1.4206
           6364.3922
              6363.7597
   2.1310
...omitted...
```

In this example, the Pn phase produced 4 distinct paths, all of which are included in the single file. The path points are now represented only by two columns containing the distances along the path from the event (in km) and radii of the points.

4. Querying a model

LLNL-Earth3D has a number of utilities to examine or extract properties from a given LLNL-G3D formatted binary model. These include tools for general model queries, extracting profiles, extracting layer information and maps.

4.1 General queries

Model layer information

Basic information about a particular model layer structure can be output to the screen with the command:

```
E3D (input command): -getlayerinfo earthmodel
```

Here is an example for the case where the LLNL-Earth3D prompt has not been established and the full model path is included:

```
java -jar LLNL-Earth3D.5.3.jar -getlayerinfo G:\PROGRAMS\EARTH3D\MODELS\LLNL-G3Dv3.e3d.binary
```

Note that the full model path is not needed if it resides in the working directory. Also, if the *earthmodel* of interest is already loaded into memory, simply execute with "-getlayerinfo" without the model name. Otherwise, the model will be loaded into memory. Example output:

```
Layer[0], LayerName= '1: Water (top)',
                                                  Max.Tess.Level= 6, Mean Radius= 6371.2212,
                                                                                                     Properties: Vp,
Layer[1], LayerName= '2: Water (bottom)',
                                                  Max.Tess.Level= 6, Mean Radius= 6368.6106,
                                                                                                     Properties: Vp,
Layer[2], LayerName= '3: Sediment 1 (top)',
                                                  Max.Tess.Level= 6, Mean Radius= 6368.6107,
                                                                                                     Properties: Vp,
Layer[3], LayerName= '4: Sediment 1 (bottom)',
                                                  Max.Tess.Level= 6, Mean Radius= 6368.3758,
                                                                                                     Properties: Vp,
Layer[4], LayerName= '5: Sediment 2 (top)',
                                                  Max.Tess.Level= 6, Mean Radius= 6368.3758,
                                                                                                     Properties: Vp,
Layer[5], LayerName= '6: Sediment 2 (bottom)',
                                                  Max.Tess.Level= 6, Mean Radius= 6367.8412,
                                                                                                     Properties: Vp,
 ...omitted...
Layer[90], LayerName= 'Inner Core (5971km)',
                                                  Max.Tess.Level= 4, Mean Radius= 400.0002,
                                                                                                     Properties: Vp,
Layer[91], LayerName= 'Inner Core (6071km)',
                                                  Max.Tess.Level= 4, Mean Radius= 299.9996,
                                                                                                     Properties: Vp,
Layer[92], LayerName= 'Inner Core (6171km)',
                                                  Max.Tess.Level= 4, Mean Radius= 199.9997,
                                                                                                     Properties: Vp,
Layer[93], LayerName= 'Inner Core (6271km)',
                                                  Max.Tess.Level= 4, Mean Radius= 99.9999,
                                                                                                     Properties: Vp,
Layer[94], LayerName= 'Inner Core (6371km)',
                                                  Max.Tess.Level= 4, Mean Radius= 0.0000,
                                                                                                     Properties: Vp,
```

Tessellation node locations

The latitudes and longitudes of the spherical tessellation grids may be output to a file with the command:

```
E3D (input command): -writelatlons maxlevel
```

where *maxlevel* is an integer of the maximum tessellation level. Note that if a model containing a tessellation grid is not already loaded into memory, the above command will need to construct a spherical tessellation grid. For example, the LLNL-G3Dv3.e3d.binary model is defined up to level 6, which consists of 40,962 vertices. To get the latitude and longitude locations of each of nodes, type:

```
E3D (input command): -writelatlons 6
```

which will create a file named "SphericalTessellationCoordinates.UpTo.Level.6.txt" with the contents that look like the following:

```
        Vertex
        Latitude
        Longitude

        0
        90.000000
        0.000000

        1
        26.719301
        72.000000

        2
        26.719301
        0.000000

        3
        26.719301
        -72.000000
```

```
26.719301 144.00000
26.719301 -144.00000
-26.719301 36.00000
-719301 -36.00000
109.00000
5
            -36.000000

20./19301 108.000000

-26.719301 180.000000

-26.719301 -108.000000

-90.000000 0.000000

∋d...
7
8
10
...omitted...
40957
                      -50.418391
                                                -144.925818
               -50.418391 -49.400876 -144.000000
40958
                     -52.462817 -143.032003
-53.490721 -144.000000
-52.462817 -144.967997
40959
40960
40961
```

General property query

Any *model_property* of interest (e.g. Vp, Vs, etc.) can be extracted using the -modelquery switch and passing a file containing a set of points to the code:

E3D (input command): -modelquery earthmodel model_property points_file

where *points_file* is a user-generated plain text file with 3 columns containing the points of interest. Each row of the *points_file* should be [*latitude longitude depth*]. The query will return a new text file that contains the original input with an addition column with values corresponding to the *model_property* value. The output file name will begin with the input file name with an added extension that corresponds to the property name. For example, we may have a file named "MyPoints.txt" which contains the entries:

30.95	40.51	10.9
40.01	30.79	2400
-29.92	-31.42	1000

The command

E3D (input command): -modelquery LLNL-G3Dv3.e3d.binary Vp MyPoints.txt

will generate a file named "MyPoints.txt.Vp" with a 4th column containing Vp values for each point like the following:

30.9500	40.5100	10.9000	6.2003
40.0100	30.7900	2400.0000	13.1993
-29.9200	-31,4200	1000.0000	11,4631

4.2 Profiles and cross sections

Extracting 1-D profiles

LLNL-Earth3D will create 1-D profiles by interpolating any model property such as Vp at any specified latitude and longitude. This is executed using the -create1dprofile command:

E3D (input command): -create1dprofile earthmodel model_property latitude longitude

The above command will output a text file named 1D_Profile_*.xy where the wildcard will consist of the model name, property and coordinates. The *.xy file will contain 2 columns which are the radii and model values.

For example, we can extract a P-wave velocity profile at latitude/longitude location of (30.5, -114.2) by typing:

```
E3D (input command): -create1dprofile LLNL-G3Dv3.e3d.binary Vp 30.5 -114.2
```

This will output a file named "1D_Profile_LLNL-G3Dv3.e3d.binary_Vp_30.5_-114.2.xy" which will look like:

6372.7738	1.5000
6372.7679	1.5000
6372.7679	3.8117
6372.7679	3.8117
6372.7679	2.4663
6372.1503	2.4663
6372.1503	4.2999
omitted	
1100.2086	11.0725
1000.1895	11.1054
900.1710	11.1352
800.1516	11.1619
700.1323	11.1854
600.1135	11.2058
500.0947	11.2230
400.0761	11.2371
300.0565	11.2481
200.0377	11.2559
100.0188	11.2606
0.0000	11.2622

Extracting 2-D profiles (cross sections) - default usage

LLNL-Earth3D will create 2-D profiles (cross sections) by interpolating any model property such as Vp along a great circle path between 2 specified latitude/longitude points. This is executed using the -create2dprofile command:

```
E3D (input command): -create2dprofile earthmodel model_property lat1 lon1 lat2 lon2
```

The above command will output a text file named 2D_Profile_*.xyz where the wildcard will consist of the model name, property and coordinates. The *.xyz file will contain 3 columns containing:

```
[profile_distance radii model_property_value]
```

where *profile_distance* is the distance (in km) from the starting point defined by *lat1* and *lon1*. The profiles will be evenly sampled in radius and in distance for compatibility with making images with GMT commands. With the default inputs, the code calculates the maximum resolution of the 3-D model and then samples the path 5 times more densely. The model is sampled at every ~5 km in radius from 6370.0 to ~3800.0 km (the crust and mantle).

For example, we can extract a P-wave velocity cross section from the latitude/longitude location of (30.5, -114.2) to (35, -116.9):

```
E3D (input command): -create2dprofile LLNL-G3Dv3.e3d.binary Vp 30.5 -114.2 35.0 -116.9
```

This will output a file named "2D_Profile_LLNL-G3Dv3.e3d.binary_Vp_30.5_-114.2_35.0_-116.9.xyz" which will look like:

```
6365.0097
   0.0000
                           6.0949
   0.0000
                           6.0949
          6360.0194
   0.0000
                           6.2045
          6355.0291
                           6.2045
   0.0000
   0.0000 6350.0388
                           6.6562
   0.0000
          6345.0485
                           6.6562
...omitted...
                      13.4572
13.4631
          3814.9709
   0.0000
   0.0000 3809.9806
   0.0000 3804.9903
                         13.4689
  23.3504 6370.0000
                           6.0980
          6365.0097
  23.3504
                           6.0980
          6360.0194
  23.3504
                           6.2039
            6355.0291
  23.3504
                           6.2039
...omitted...
 560.4085
            3814.9709
                          13.4601
                          13.4668
            3809.9806
 560.4085
 560.4085
            3804.9903
                          13.4735
```

In addition, files containing the radii of each model layer along the great circle path will be output to files named:

```
"Layer_0_LLNL-G3Dv3.e3d.binary_30.5_-114.2_35.0_-116.9.xy"
"Layer_1_LLNL-G3Dv3.e3d.binary_30.5_-114.2_35.0_-116.9.xy"
...
"Layer 94 LLNL-G3Dv3.e3d.binary 30.5 -114.2 35.0 -116.9.xy"
```

Each of the above files will have 2 columns containing [profile_distance radii] for plotting overlays of the undulating model surfaces if desired (possibly included in a GMT script).

Extracting 2-D profiles (cross sections) - set radial limits

The default radius range (in the example above) spans crust and mantle. If it is desired to expand or restrict the radius, simply add 2 additional terms with the minimum radius (*minrad*) and maximum radius (*maxrad*):

E3D (input command): -create2dprofile earthmodel model_property lat1 lon1 lat2 lon2 minrad maxrad

Extracting 2-D profiles (cross sections) - set radial sample rate

The cross section output can be further refined by changing the vertical (radial) sample rate by including an additional number (*delta*) which defines the distance between points in km:

E3D (input command): -create2dprofile earthmodel model_property lat1 lon1 lat2 lon2 minrad maxrad delta

Extracting 2-D profiles (cross sections) - return percent perturbations

The default values returned are returned in an absolute sense (e.g. absolute Vp, Vs, etc.). An alternative output is in terms of percent perturbation relative to the mean value in each layer. This is done by adding the flag "-dpct" to the end of the -create2dprofile command:

E3D (input command): -create2dprofile earthmodel model_property lat1 lon1 lat2 lon2 -dpct

Note that values in the sedimentary and crustal layers can be very high and some values may be meaningless if there is zero thickness.

4.3 Map output

LLNL-Earth3D may be used to extract map data for a specified *model_property* using the -createmap command:

E3D (input command): -createmap earthmodel model_property minlat minlon maxlat maxlon layerindex

where *minlat/minlon* defines the lower left-hand corner of the map region, *maxlat/maxlon* defines the upper right-hand corner of the bounded region, and *layerindex* is the model layer index (beginning with index 0). *Hint:* Use the -getlayerinfo command to get the index number of the layer desired.

The above command will output a text file named Map_*.xyz where the wildcard will consist of the model name, property and bounding coordinates. The *.xyz file will contain 3columns which are:

[latitudes longitudes model_values].

For example, the following command creates a map data file containing absolute P-wave velocity for layer index 16 in the LLNL-G3Dv3 model:

E3D (input command): -createmap LLNL-G3Dv3.e3d.binary Vp 15.0 30.0 45.0 90.0 16

This will create a file named "Map_LLNL-G3Dv3.e3d.binary_Vp_16_15.0_30.0_45.0_90.0.xyz" which will have 3 columns with the latitudes, longitudes and Vp values:

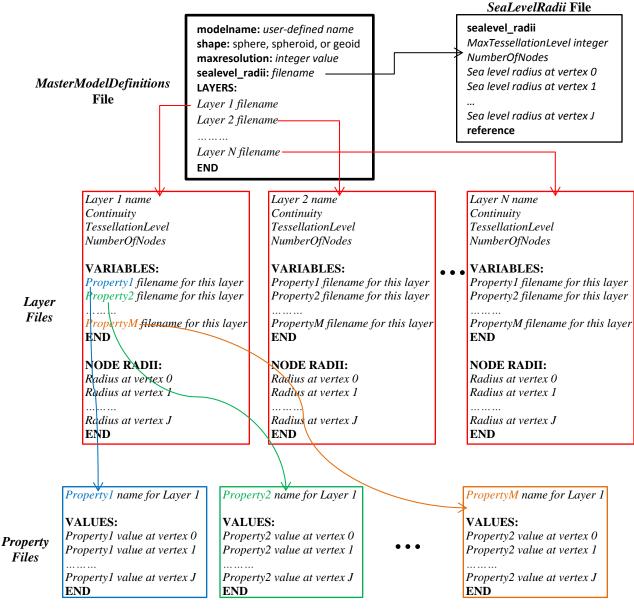
30.0000 30.2166	8.0701 8.0707
30.4332	8.0714
89.5668	8.0778
89.7834	8.0787
30.0000	8.0719
30.2166	8.0726
89.3502	8.1448
89.5668	8.1401
89.7834	8.1376
	30.2166 30.4332 89.5668 89.7834 30.0000 30.2166 89.3502 89.5668

5. Model importation

LLNL-Earth3D is specifically designed to work with LLNL-G3D formatted Earth models stored in a binary stream. It is possible to import alternative Earth models and/or potentially use LLNL-Earth3D as a lookup table for user-defined variables with a quasi-spherical spatial arrangement. Since our primary focus is on structural models of the Earth, the following text specifically describes how to import an Earth model.

Hierarchical file scheme

Constructing a LLNL-G3D formatted binary file is achieved by first constructing several plain text files. The text files include i) a *MasterModelDefinitions* file with the top-level information about a model, ii) *LayerFiles* containing information about specific layers defined in the master file, iii) *PropertyFiles* with model values for a specific property (e.g. Vp) in a specific layer, and iv) *SeaLevelRadii* file containing the radii corresponding to sea level at nodes defined by the spherical tessellation grids. Below is a schematic of the file structure:



MasterModelDefinitions file content

In the *MasterModelDefinitions* file shown in the schematic (as well as the other files), the values in **bold** font are needed verbatim and the values in *italics* are user-defined inputs. The text needed in the *MasterModelDefinitions* file is simply the name of the model to construct, the general model shape, the maximum tessellation level and file names. The model name can be anything the user chooses, but the shape of the model being created must be one of the 3 option listed in the schematic. In any case, the user must define the radii corresponding to sea level and the file name should be listed. Here is an example for the LLNL-G3Dv3 model build:

modelname: LLNL-G3Dv3
shape: geoid
maxresolution: 6
sealevel_radii: sealevel_radii.ascii.dat
LAYERS:
LAYER.1.1.ascii.dat
LAYER.1.2.ascii.dat
LAYER.1.3.ascii.dat
LAYER.1.4.ascii.dat
LAYER.1.5.ascii.dat
LAYER.1.5.ascii.dat
LAYER.3.35.ascii.dat
LAYER.3.35.ascii.dat
LAYER.3.35.ascii.dat
LAYER.3.36.ascii.dat
LAYER.3.37.ascii.dat

LAYER.3.38.ascii.dat

The layer file names must be in order from the top down (surface to the bottom of the model) and the radii of any defined layer may not be greater than the radii of any layer listed above it (no crossing surfaces). However, the layers may "pinch out" and have the same radii as the layer above. Note that the layer file names may be anything the user chooses. The layer names in the example above are our personal nomenclature. Additionally, file system paths may be included if the files reside in different locations or sub-directories (e.g. G:\MyModel\Layer1.1\Layer1.1.ascii.dat).

Node ordering

Each model property (e.g. Vp, Vs, surface radii) must be defined at a specific set of latitude-longitude points determined by the spherical tessellation recursion process. The model values listed in the *SeaLevelRadii* file and the *PropertyFiles* must be interpolated by the user to each of these points and written to the text files in a precise sequence. To get a list of the sequence of hard-wired latitude-longitude points, type:

E3D (input command): -writelatlons maxlevel

This will create a text file with the latitude-longitude locations of the tessellation node points for a grid defined at the requested maximum tessellation level. The number of node points for a particular tessellation level can also be determined from the output.

Note that the sequence of the latitude-longitude points never changes, regardless of the tessellation level requested. Instead, points belonging to higher tessellation level grids are appended to the bottom of the list of points from the lower level grids.

SeaLevelRadii file

The *SeaLevelRadii* file is a user-defined file containing the radii corresponding to a reference whereby depth is measured (the reference radius is often sea level). The text file must contain a header line, followed by the maximum tessellation level, and the number of nodes. The radius values are then listed in the sequence of latitude-longitude points defined by the spherical tessellation recursion process.

Here is an example for the LLNL-G3Dv3 build where the sealevel_radii file was named "sealevel radii.ascii.dat" according the *MasterModelDefinitions* file:

sealevel_radii 6 40962 6356.765920 6373.798596 ...omitted... 6364.343637 6364.713855 reference

Layer files

The LayerFiles contain information about each of the layers in the model. The header includes a user-defined layer name and a Continuity descriptor that identifies whether the layer (or surface) is continuous or discontinuous. The next 2 header entries are the tessellation level and number of points, similar to the entries in the SeaLevelRadii file. Note that the resolution (or tessellation) level may differ for each of the layers.

There are 3 possible values for *Continuity*: i) "continuous" if the surface is not at a discontinuity, ii) "top" if the surface is the top-side of discontinuity, or iii) "bottom" if the surface is the underside of a discontinuity. An example of a "top" is a layer defined at the Moho and with model properties corresponding to the bottom of the crust (possible model property might be Vp with values near 6.5 km/s). An example of a "bottom" is a layer defined at the Moho and with model properties corresponding to the top of the mantle (possible model property might be Vp with values near 8.0 km/s). Note that to properly form a discontinuity, the radii of each of the "top" and "bottom" surfaces should be exactly the same.

<u>Note:</u> In order to specify some particular phases for 3-D ray tracing, certain layer names (designated in the first line of header) **must** contain specific strings that identify them as special layers. The strings can be upper or lower case, and may be anywhere in the name of the layer. The current list of special layer names currently include: "water", "upper crust", "lower crust", "moho", "transition zone", "CMB", and "ICB". These special strings can be in the layer name of a discontinuity top or bottom (or both). Currently there is no specific designation for the "410" or "660", just identify all layers in the transition zone with "transition zone" in the name.

Following the header information is a list of filenames containing the model properties (or variables) associated with a given layer. The user may include any properties (Vp, Vs, Q, etc.), but note that it is expected that each layer have the same collection of associated properties.

Following the list of model property file names is a list of node radii values for each of the vertices. The radii are defined from the center of the Earth to the latitude-longitude points defined in the -writelatlons output file described above.

Below, we will show some example layer file contents for the LLNL-G3Dv3 P-wave model where we are also including some S-wave velocities for demonstration. The LLNL-G3Dv3 model is defined at tessellation level 6 (~1° node spacing) in the crust and upper mantle. In the lower mantle however, the maximum tessellation level is 5 (~2° node spacing).

Here is an example layer file contents for the first layer in the model which defines the top of the water layer:

```
1: Water (top)
bottom
6
40962

VARIABLES:
LAYER.1.1.Vp.ascii.dat
LAYER.1.1.Vs.ascii.dat
END

NODE_RADII:
6356.765920
6374.044134
6374.112587
...omitted...
6364.343637
6364.713855
END
```

In the example shown above, notice that we include the string "Water" in the name so that particular seismic phases can be ray traced (e.g. we can compute both pwP and pP). The top of the water is a discontinuity due to the air-water interface and it thus a "bottom" since it is the underside of that discontinuity. The file names for the variables (properties) are clearly pointing to files with Vp and Vs values, but there is no file naming convention required by the code.

The next example is a layer file for the bottom of the lower crust:

```
14: Lower Crust (bottom) top 6 40962

VARIABLES: LAYER.1.14.Vp.ascii.dat LAYER.1.14.Vs.ascii.dat END

NODE_RADII: 6343.987562 6336.362607 ...omitted... 6354.162211 6354.238545
```

In the example above, the bottom of the lower crust is a discontinuous "top" since it is the top side of the Moho discontinuity.

The next example is the layer file contents for the layer also at the Moho, but representing the top of the upper mantle:

```
15: Top of mantle (Moho) bottom
6
40962

VARIABLES:
LAYER.1.15.Vp.ascii.dat
LAYER.1.15.Vs.ascii.dat
END

NODE_RADII:
6343.987562
6336.362607
...omitted...
6354.162211
6354.238545
END
```

Notice that in the above example, we include the string "Moho" in the layer name so that this surface may be identified when computing certain seismic phases such as Pn and PmP. Also notice that the radii are exactly the same as the previous example which is the layer file for the bottom of the lower crust.

The next example is the layer file contents for a lower mantle surface at approximately 971 km depth:

```
4: Lower Mantle (971km) continuous 5 10242 VARIABLES: LAYER.2.4.Vp.ascii.dat LAYER.2.4.Vs.ascii.dat END NODE_RADII: 5389.017000 5402.192897 ...omitted... 5394.890116 5395.456085 END
```

In the example above, the layer is not a discontinuity and is therefore marked "continuous". In addition, this layer is defined at a lower resolution level than the previous example (tessellation level 5 rather than 6). The layer name contains a "4" since this is the 4th lower mantle layer. This is our personal layer naming convention and thus has no particular significance to the user.

Property (or Variable) files

The *PropertyFiles* are simple text files containing the name of the properties and actual model values such as Vp. The top line of the file should be the name of the property which is user-defined. It should

be noted that, if the user wishes to execute ray tracing utilities, Vp and/or Vs must be one of the properties and the name given to these properties must be exactly "Vp" and/or "Vs".

Here is an example property for the LLNL-G3Dv3 mantle P-wave velocity at the Moho:

Vp
VALUES:
8.146360
8.198282
8.119254
8.172410
...omitted...
8.035326
8.017037
8.016469
8.020075
END

Again, the model property values are listed in the precise sequence of the latitude-longitude points listed by the -writelatlons command.

Execution

Once the collection of text files are completed, the model importation process may be initiated using the LLNL-Earth3D -importmodel command as follows:

E3D (input command): -importmodel MasterModelDefinitions

where *MasterModelDefinitions* is a user-defined filename. The process will compute a spherical tessellation grid at the highest tessellation level needed and populate a binary stream with complete model information. The code will also compute and store normal vectors to surfaces that are listed as discontinuous for the purpose of more efficient ray tracing.

If Vp and/or Vs are included as properties, velocity gradients will be computed at each point in the model and stored with the model. This pre-computation increases the efficiency of the ray tracing algorithms. Note that the pre-computation steps could take substantial amounts of time, which is a function of the total number of model nodes. For example, the LLNL-G3Dv3 P-wave velocity model consists of ~1.6 million points and takes ~1.5 hours to complete on a moderate PC workstation.